

# LIMITS OF AGREEMENT METHOD FOR COMPARING PAVEMENT FRICTION MEASUREMENTS

*Presented by*

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# Overview of Presentation

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Objectives



Methods



Background



Tests results



Conclusions

# Objectives

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- **Pavement friction equipment comparisons: which is the equivalent value (Harmonization)**
- **LOA method – Bland & Altman 1986**
  - **Define “a priori” boundaries (limits)**
  - **These limits are defined by the use of the measurements**
  - **Should it replace the use of correlations?**

# Objectives

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- **Illustrate the use of LOA to compare two pavement friction devices based on agreement**
- **Good agreement allows interchangeability**
- **Is good agreement always possible?**
- **3 Examples**

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# Methods: LOA

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- Assuming Normal Distribution, for 95% confidence,  $z = 1.96 (\approx 2)$
- Repeatability  $r_i = 1.96\sqrt{2}s_i = 2.77\sqrt{s_i^2}$ 
  - $r_1$  and  $r_2$ , for each device, respectively
- Limits of Agreement (LOA) between the two devices
$$LOA = 1.96\sqrt{s_c}$$
- Can it replace reproducibility (R)?

# Methods: LOA

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- **Limits of Agreement (Bland & Altman)**
- **Three components: combines variability of each device (2) and third one capturing their interaction**

- **Variances:**

$s_1^2$  var device1,  $s_2^2$  var device2, and  $s_D^2$  var interaction

- **Combined effects:**

$$s_c = \sqrt{s_D^2 + |f_1| s_1^2 + |f_2| s_2^2}$$

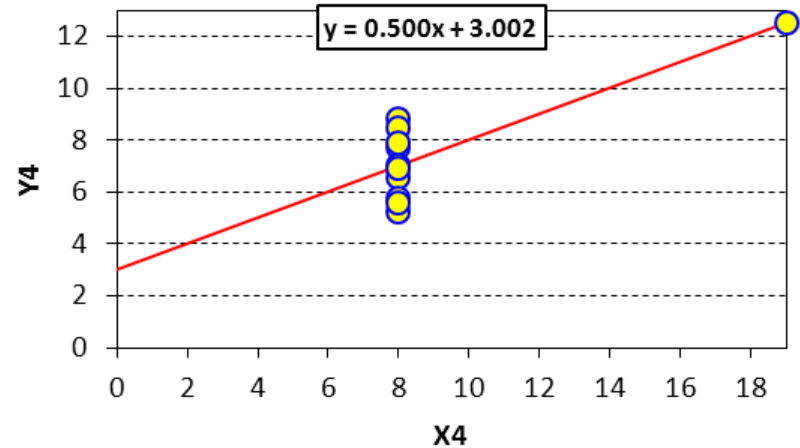
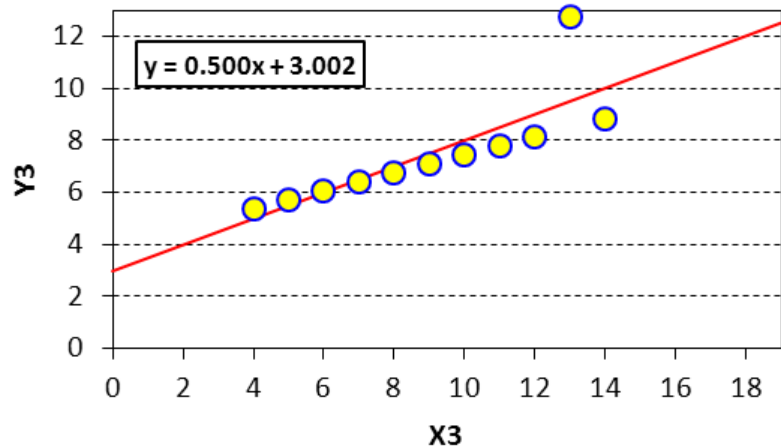
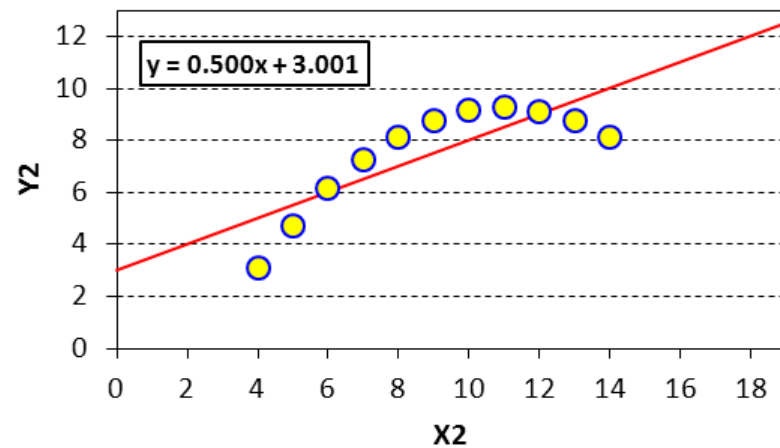
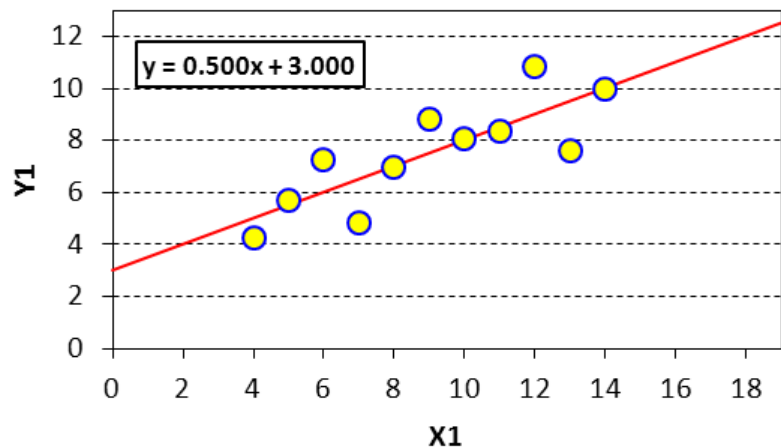
$$f_1 = \left(1 - \frac{1}{m_1}\right) \quad f_2 = \left(1 - \frac{1}{m_2}\right) \quad f = \left(1 - \frac{1}{n} \sum \frac{1}{m_i}\right)$$



# Methods

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- **Francis Anscombe, Princeton professor and statistician**
- **Anscombe Quartet**
  - $X_{\text{mean}} = 9.00, \text{var}_x = 11.0$
  - $y_{\text{mean}} = 7.50, \text{var}_y = 4.1$
  - **Correlation between  $x$ - $y = 0.816$**
  - **Linear regression:  $y = 0.500 x + 3.00$**
- **Importance of graphing and the effect of outliers on statistical properties**



# Overview of Presentation

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# NASA Wallops Island Flight Facility





# Virginia Smart Road



VTTI and labs

Sections  
Loop-A-B-C-D

Sections  
E-F-G-H-J-I-K-L

PCC, HFS  
and bridges



# Locked-wheel skid tester



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# Grip Tester (fixed slip)





# Dynatest HFT (fixed slip)





# Dynamic Friction Tester



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# Overview of Presentation

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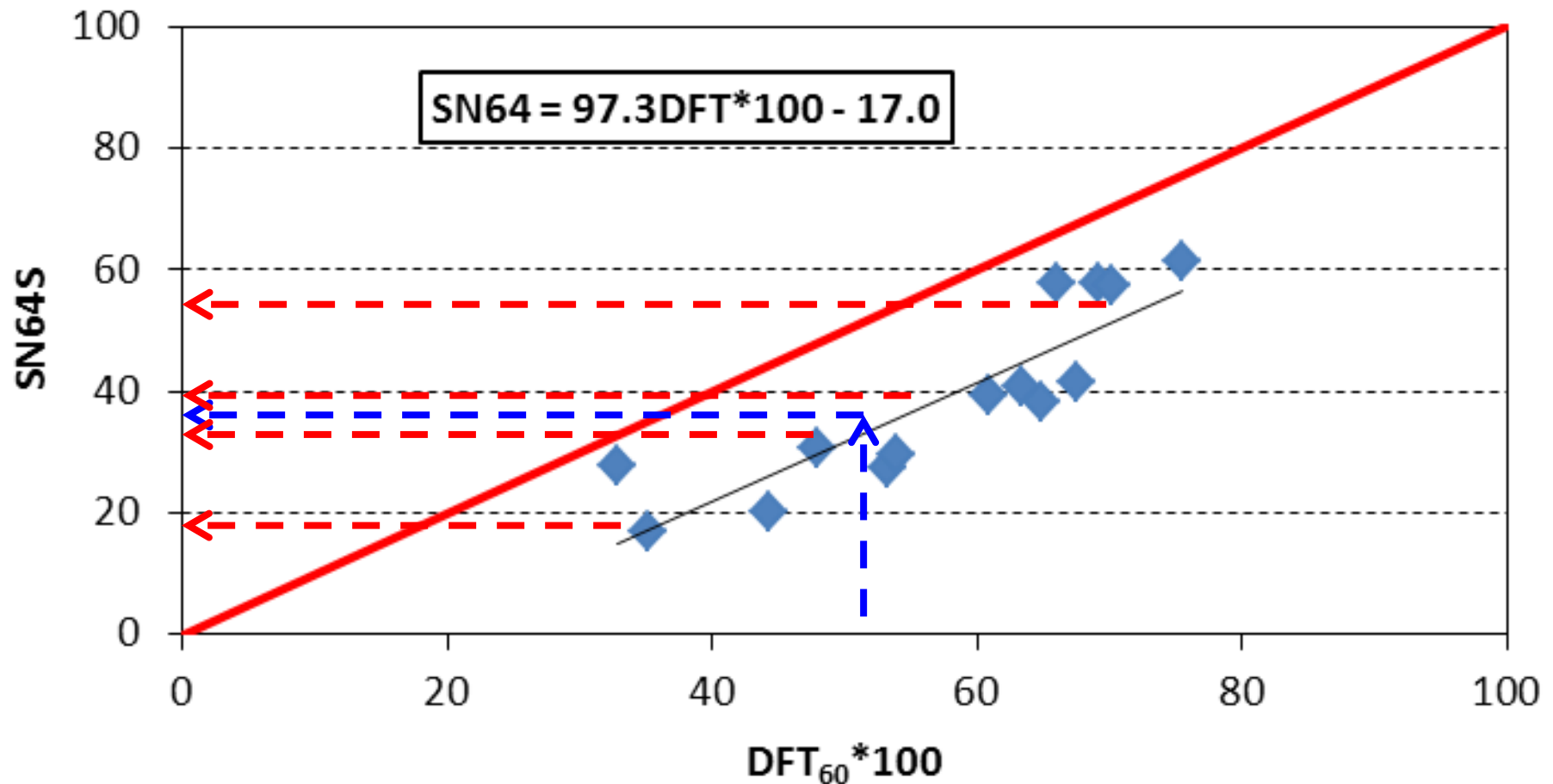
Tests results



Conclusions

# Example 1:

Wallops SN64S-DFT<sub>60</sub>\*100



# Example 1: For 4&8 runs

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- **Variances:**  $s_1^2 = 5.181$ ,  $s_2^2 = 5.94$ , and  $s_D^2 = 70.144$

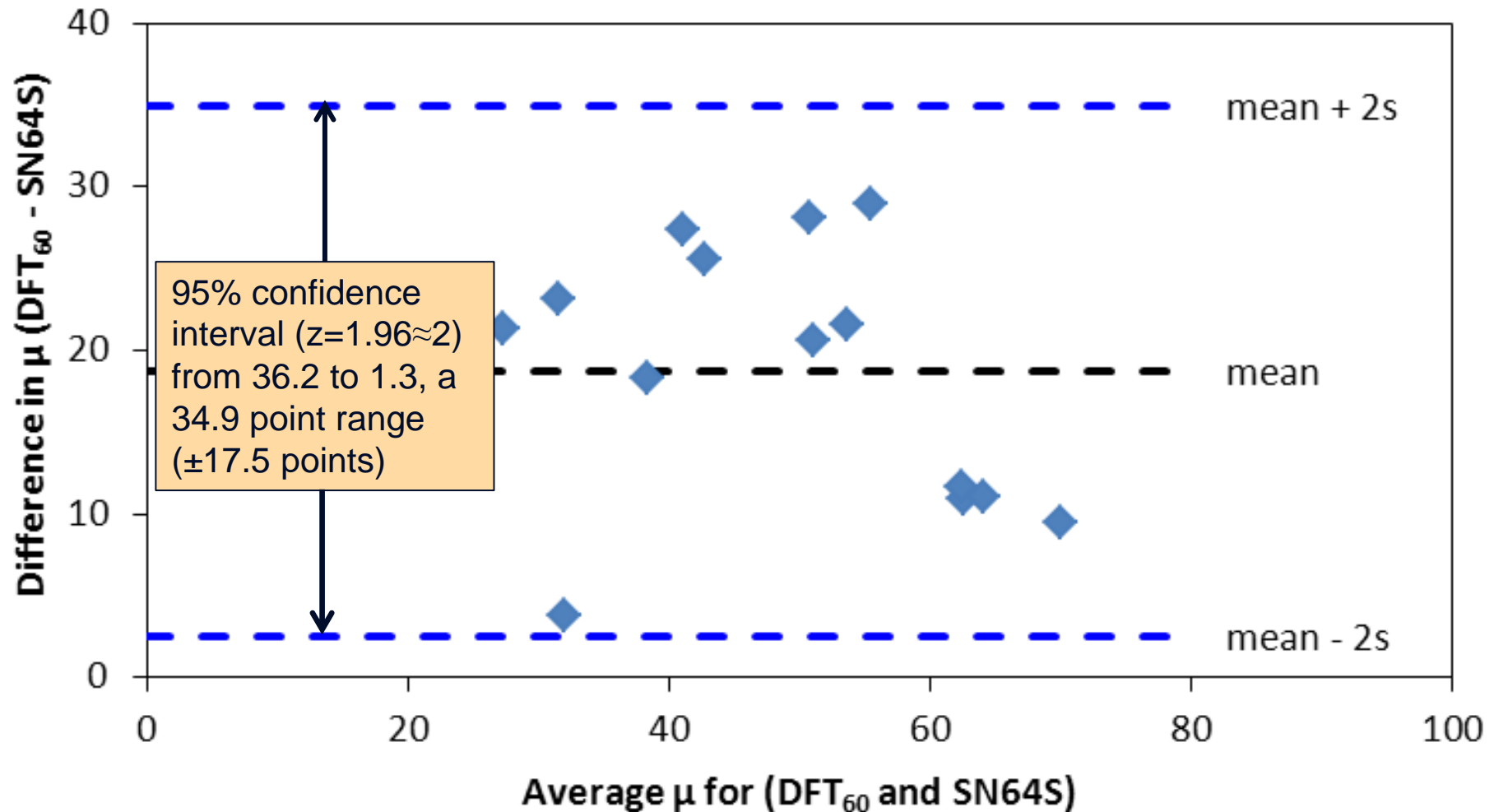
$$f_1 = \frac{3}{4}, f_2 = \frac{7}{8}$$

- **Combined effects:**

$$s_c = \sqrt{70.144 + \frac{3}{4} \times 5.181 + \frac{7}{8} \times 5.94} = 8.9$$

- **LOA:  $\pm 17.5$ , range 34.9 points**
- **Repeatability,  $r_{1DFT_{60}} = 6.3$  &  $r_{2SN64S} = 6.8$**

# Example 1:





# Example 2: Different Agreements

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- **Three fixed-slip devices:**
  - **GT1 = Grip Tester 1,**
  - **GT2 = Grip Tester 2 and,**
  - **HFT = Dynatest HFT.**
- **Three speeds (25, 40, and 55 mph)**
- **Three water film thickness (0.25, 0.5, and 1.0 mm)**
- **Same wheelpath and 6% grade**

# Testing same wheel path



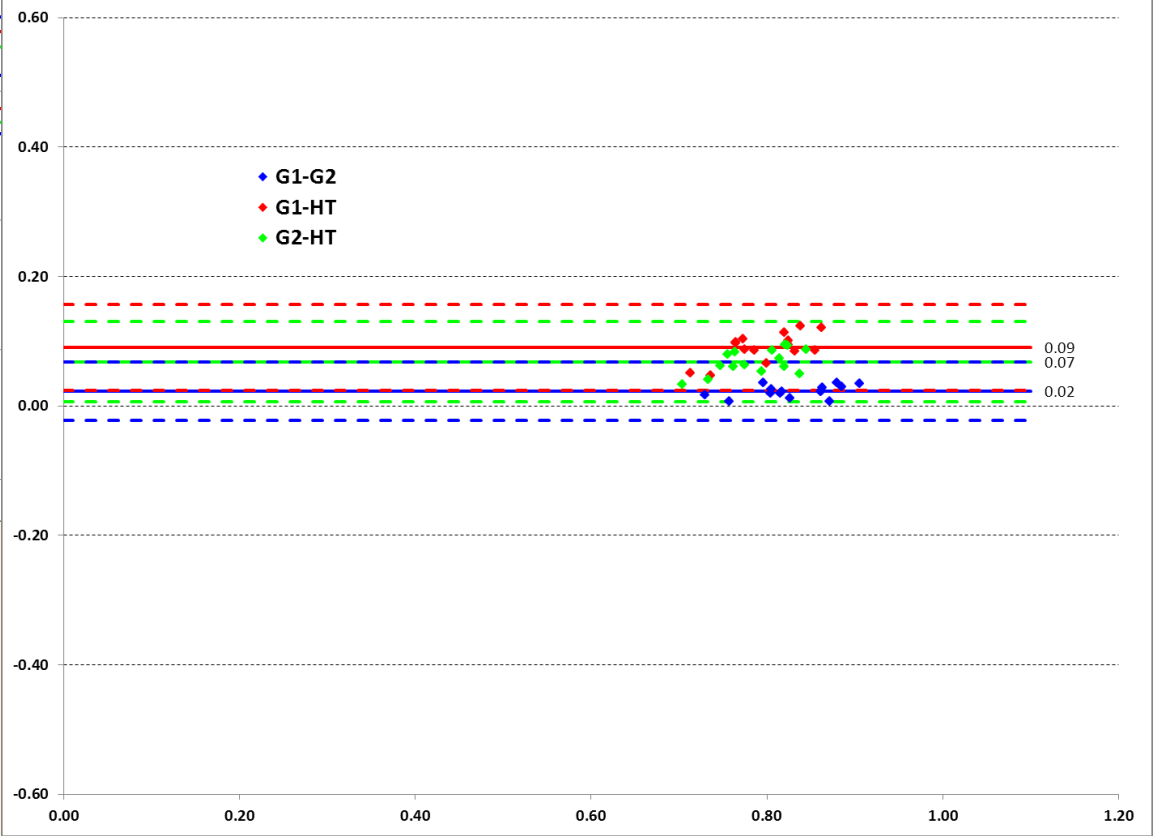
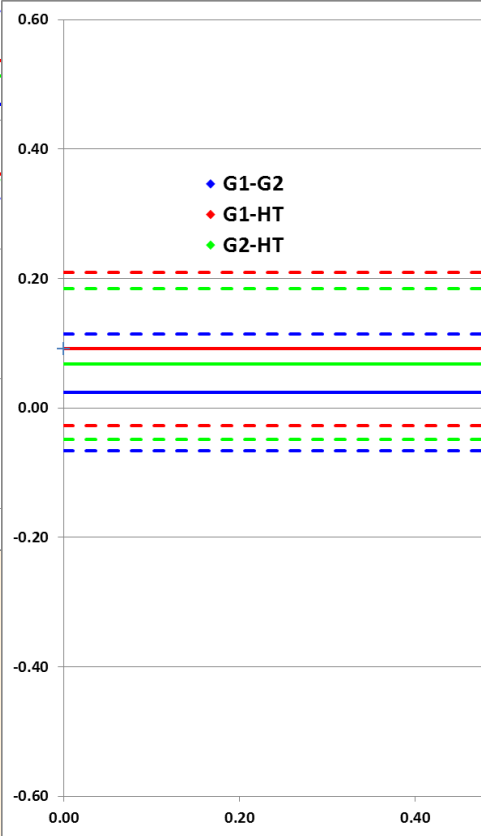
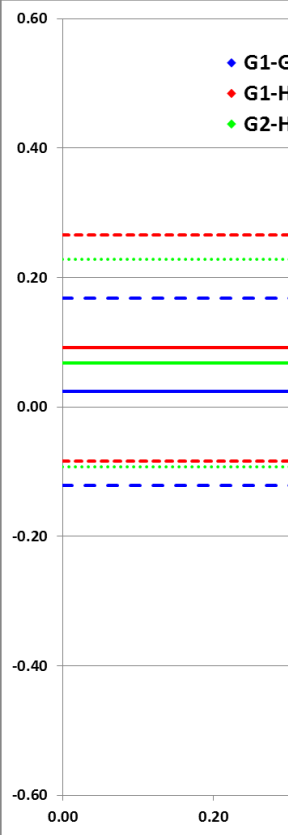
# Example 2

Effects of speed change between units			
		40 mph	
DOWNHILL	GT1-GT2	GT1-HFT	GT2-HFT
Limits of Agreement: 3 feet	0.14	0.17	0.16
Limits of Agreement: 30 feet	0.09	0.12	0.12
Limits of Agreement: 300 feet	0.05	0.07	0.06
UPHILL			
Limits of Agreement: 3 feet	0.20	0.19	0.19
Limits of Agreement: 30 feet	0.12	0.14	0.12
Limits of Agreement: 300 feet	0.05	0.07	0.07





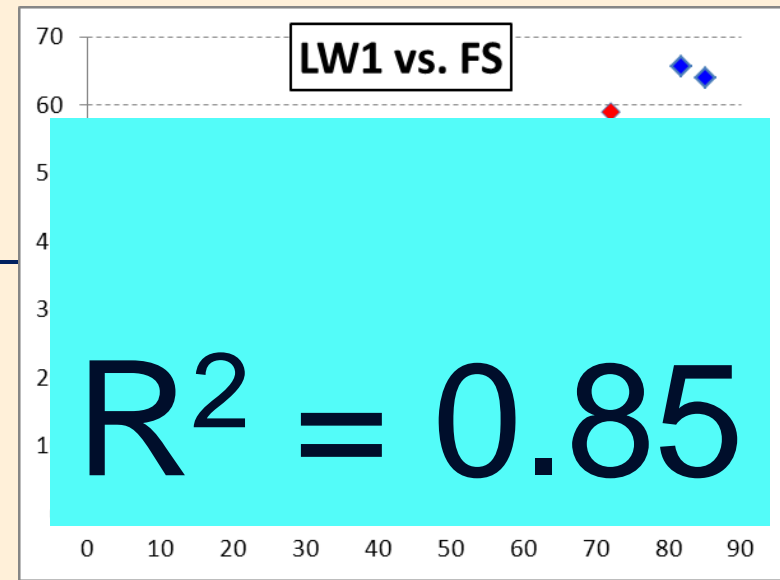
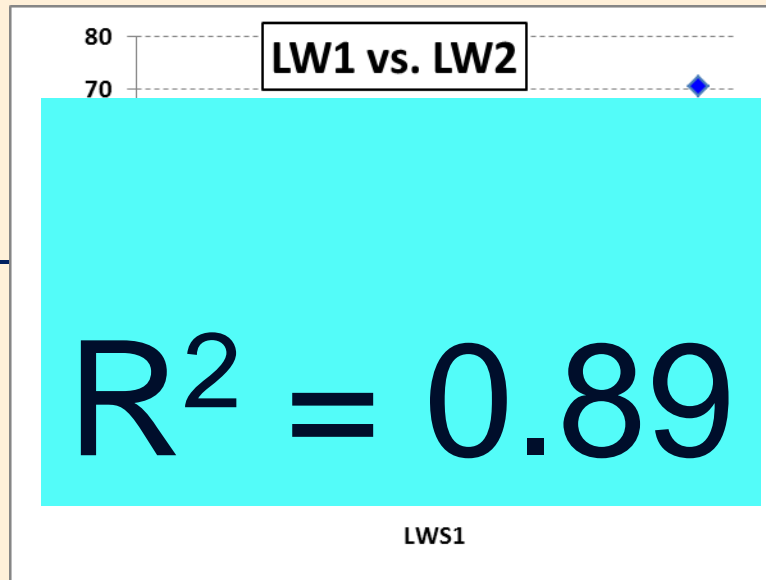
Effects of speed change between units	40 mph		
	GT1-GT2	GT1-HFT	GT2-HFT
<b>DOWNHILL</b>			
Repeatability factor $r_1$ :	0.04	0.04	0.04
Repeatability factor $r_2$ :	0.04	0.06	0.06
Limits of Agreement: 300 feet	0.05	0.07	0.06
<b>UPHILL</b>			
Repeatability factor $r_1$ :	0.05	0.05	0.04
Repeatability factor $r_2$ :	0.04	0.07	0.07
Limits of Agreement: 300 feet	0.05	0.07	0.07



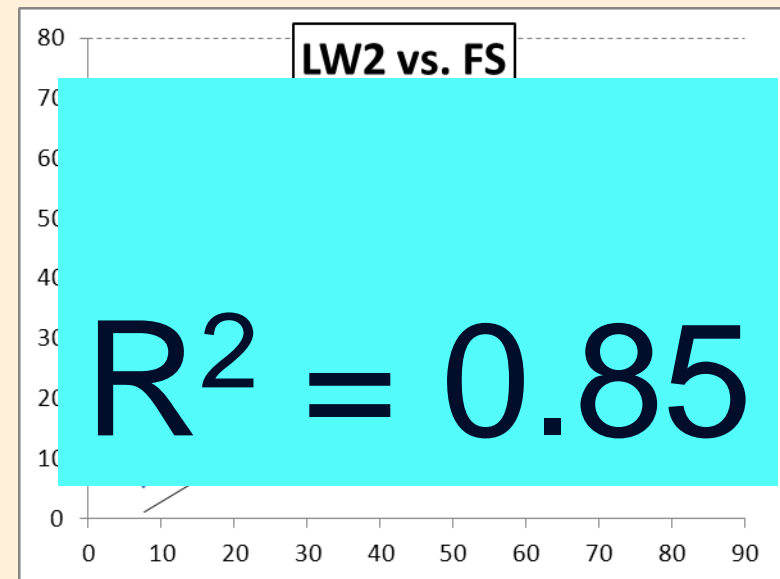
# Example 3

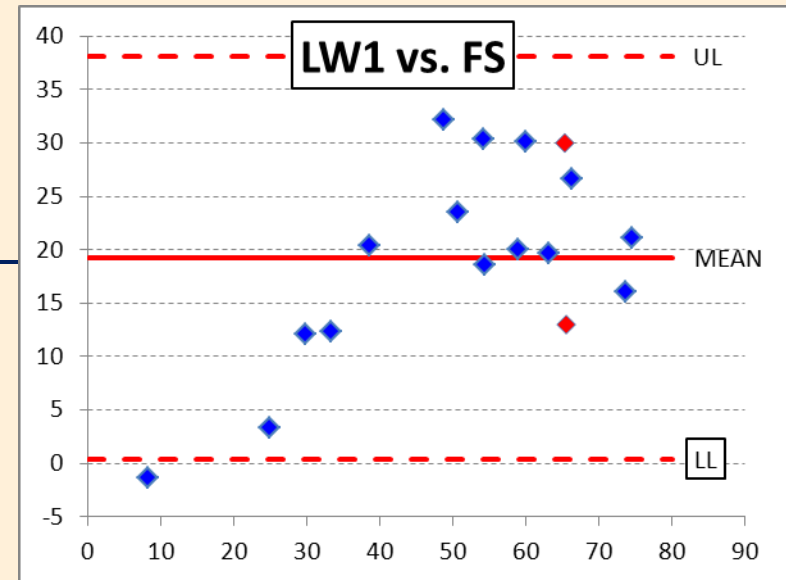
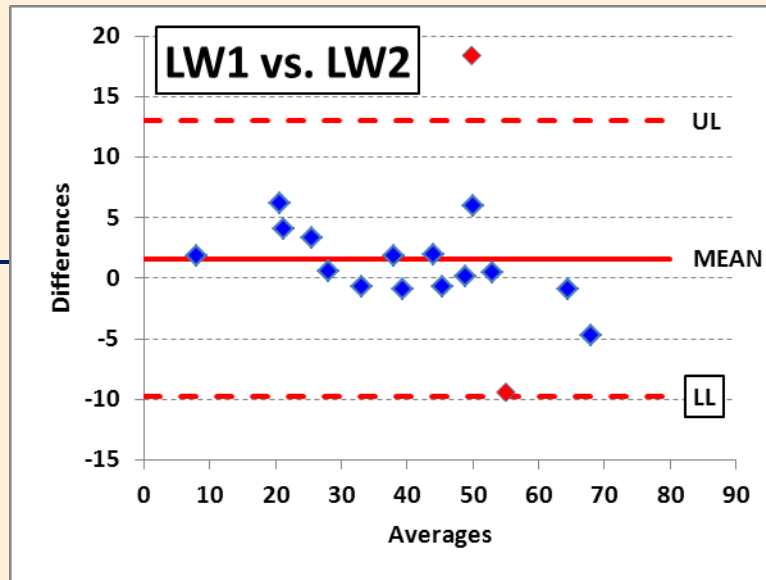
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- **Two locked-wheel skid testers and one fixed-slip device**
  - **LWS1**
  - **LWS2**
  - **FS**
- **Average data only (no repeatability)**
- **LOA effect on statistical inferences**

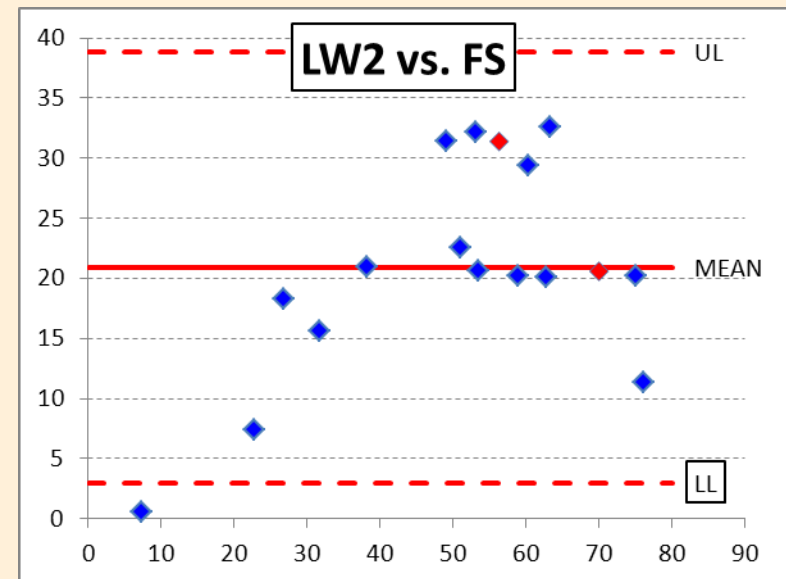


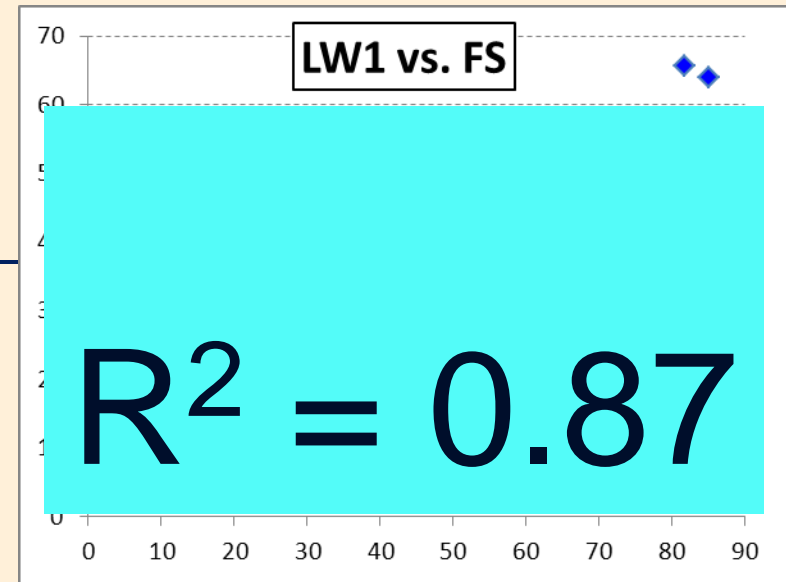
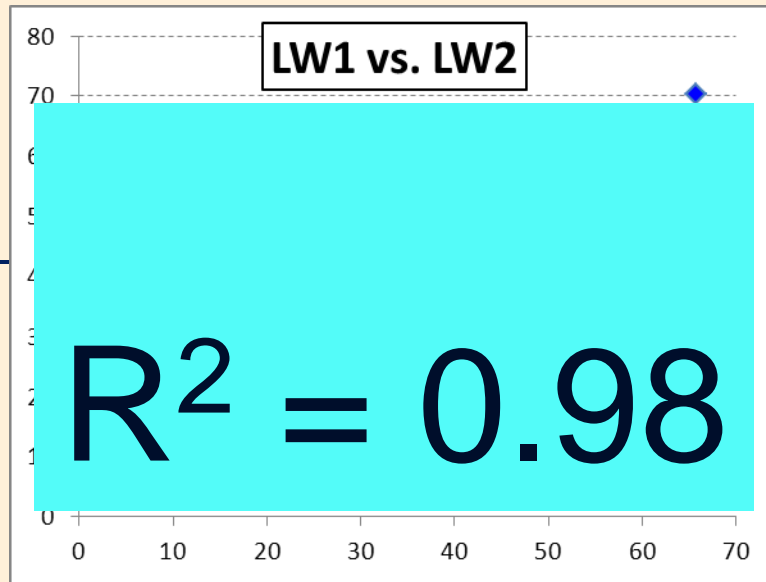
- Analysis based on averages
- Good correlations
- Two outliers



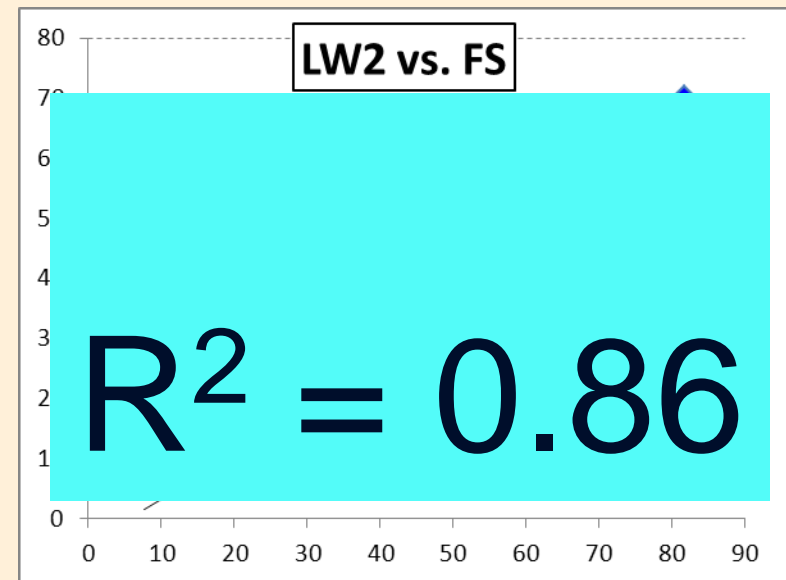


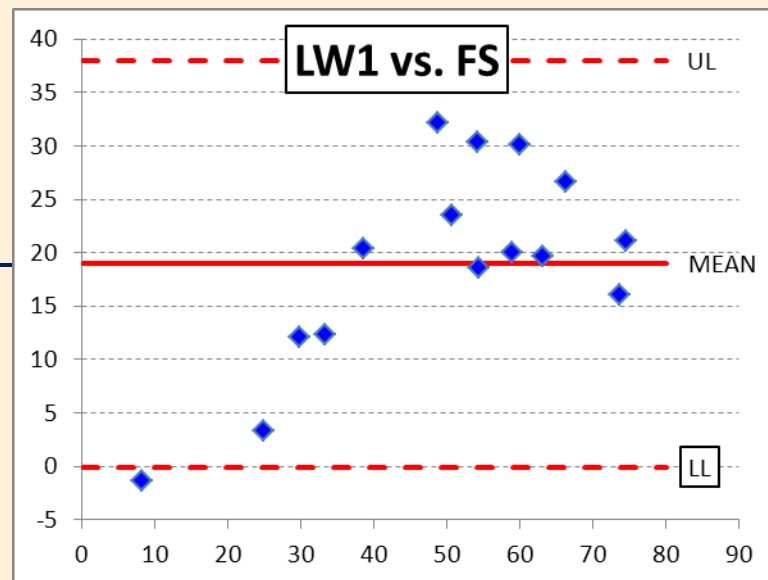
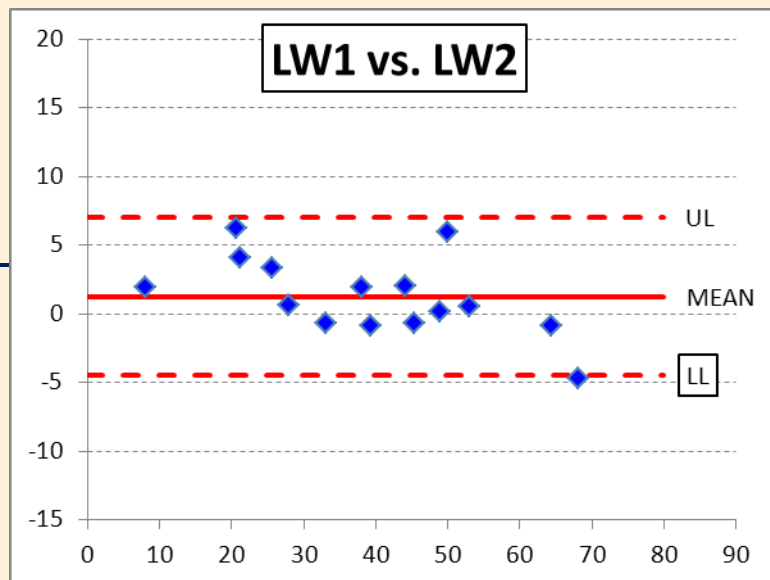
- Plotting average vs. differences (LOA)
- LWS1-LWS2: 22.8
- LWS1-FS: 37.7
- LWS2-FS: 35.8



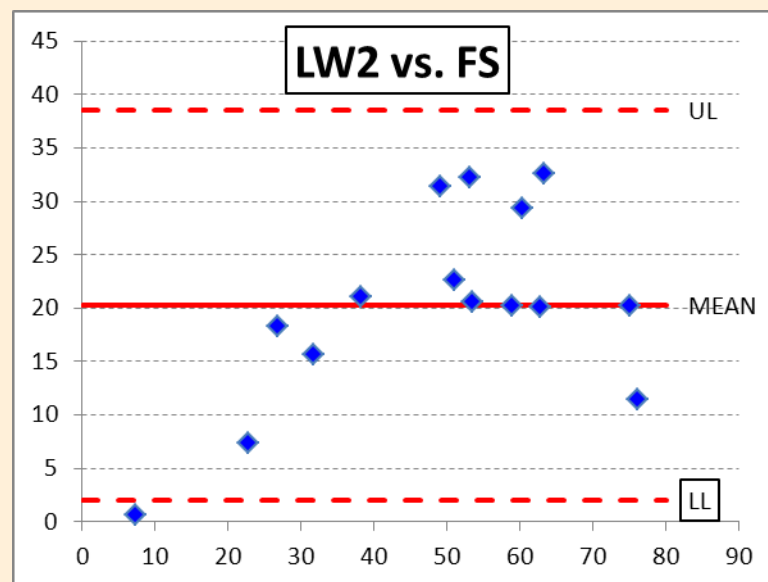


- Removing the outliers
- Better correlation for LWS1 and LWS2, the other two, minimal effect





- Limits of Agreement
- LWS1-LWS2: 11.5 (22.8)
- LWS1-FS: 38.1 (37.7)
- LWS2-FS: 36.5 (35.8)



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# Conclusions

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- **Proposed a method to compare the repeatability and a new alternative for the reproducibility factor, known as the Limits of Agreement**
- **More research is proposed to explain the effect of the factors that introduce variability and for accountability**
- **Important to check for normality**
- **Use of correlation is inappropriate!**

# Questions: [edeleoni@vt.edu](mailto:edeleoni@vt.edu)



**MCF**  
Marilyn Chase Foundation  
Dedicated to the continuing education of children's literature with the  
Marilyn Chase and Bruce Brown  
to memory of Marilyn  
Given to the Town of Chittenden and the children of the world  
June 14, 2008  
to the Marilyn Chase Foundation, Inc. on the occasion of the  
fortieth anniversary in 2007 of the publication of the book  
"Story of Chittenden"  
The foundation was formed because of the memory of a little girl who  
loved to read, who had been orphaned with her parents early in the  
year and expressed her hope that the legacy of "Story" would be her name.  
Therefore, Marilyn will live through the readers of  
The Story of Chittenden Foundation, Inc.  
Marilyn Chase's Parents  
Peter Chase, Treasurer and Elizabeth Chase, Secretary

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