



# Investigation of Profile-Based Curl and Warp Analysis Using LTPP Profile Data

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#### AZ Section 040213, Upward Curl



Source: FHWA **PE 2019** 



#### Advancement of Curl and Warp.....

- Estimate the level of curl and warp of JPCC using profile.
- Relate curl and warp to roughness.
- •Refine an existing method.
- Apply the method to a broader set of sections.

"What would the roughness be without curl and warp?"



#### Core Method (Chang, Rasmussen, et al.)

- Locate the joints.
- Isolate slab profiles.
- Fit slab profiles to an assumed function (Westergaard).
- Cast the result in terms of strain gradient.
- Aggregate over a test section.



### Joint Finding



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#### **Isolated Slab Profile**



Source: FHWA-HRT-12-068



#### Fitted Slab Profile



Source: FHWA-HRT-12-068





#### Westergaard Model

$$z = -z_0 \frac{2 \cos \lambda \cosh \lambda}{\sin 2\lambda - \sinh 2\lambda} \left[ (-\tan \lambda + \tanh \lambda) \cos \frac{x}{l\sqrt{2}} \cosh \frac{x}{l\sqrt{2}} + (\tan \lambda + \tanh \lambda) \sin \frac{x}{l\sqrt{2}} \sinh \frac{x}{l\sqrt{2}} \right]$$
$$+ (\tan \lambda + \tanh \lambda) \sin \frac{x}{l\sqrt{2}} \sinh \frac{x}{l\sqrt{2}} \right]$$
$$\lambda = \frac{b}{l\sqrt{8}} \qquad l = \sqrt[4]{\frac{Eh^3}{12(1-\mu^2)k}} \qquad z_0 = \frac{-(1+\mu)(\alpha \Delta T + \Delta \varepsilon_{sh})}{h} l^2$$

$$PSG = \frac{(\alpha \Delta T + \Delta \varepsilon_{sh})}{h}$$



#### **Idealized Slab Shapes**



Source: Rasmussen





#### Structural Evaluation, Spatial Trends

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#### Structural Evaluation, Trends Over Time





#### Structural Evaluation, by Test Section





#### IRI Versus PSG, Hypothesis



TRB 2008, Session 573



#### IRI Versus PSG, Hypothesis



TRB 2008, Session 573



#### Idealized Profile (l = 40 inches)





#### IRI versus PSG



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#### IRI/PSG Slope





#### Uplift and PSG

$$z(x) = z_0 f(x,l,b) = -PSG(1+\mu)l^2 f(x,l,b)$$

$$\Delta z = z(b/2) - z(0) = -PSG(1+\mu)l^2 \left(1 - \frac{s_{\lambda}ch_{\lambda} - c_{\lambda}sh_{\lambda}}{s_{\lambda}c_{\lambda} - sh_{\lambda}ch_{\lambda}}\right)$$



#### **IRI Versus Uplift**





#### Idealized Curl and Background Roughness



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#### Idealized Curl and Background Roughness



#### Idealized Curl and Background Roughness

$$IRI_{Comb} = \sqrt{IRI_{Curl}^2 + IRI_{Back}^2}$$

$$IRI_{Comb} = \sqrt{\left(PSG\frac{dIRI}{dPSG}\right)^2 + IRI_{Back}^2}$$



#### **Background Roughness**

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$$IRI_{Back} = \sqrt{IRI_{Comb}^2 - A\left(PSG\frac{dIRI}{dPSG}\right)^2}$$



Read Profile User's Group

#### Section-Wide PSG Average





#### IRI versus PSG, FHWA Data







#### IRI versus Uplift, FHWA Data



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#### IRI versus Uplift, LTPP Data





#### IRI versus Uplift, LTPP Data





#### Assessment

- The fitted values relating IRI to uplift were not systematically related to the theory.
- This could be caused by:
  - The structural model.
  - The "sum of squares" model.
  - The low number of slabs per section.
  - Some other thing I haven't noticed.



Possible Next Steps...

- •Notice something new.
- Difference profiles.
- Spectral methods.
- Specialized filters.
- "Advanced" methods.



#### The Report.....

is in the editing phase.

## Thank you!!!!



