

Pavement Evaluation 2019



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Roanoke, Virginia

# Road Surface Measurement Spacing Based on Delaunay Triangulation

By

Craig Altmann

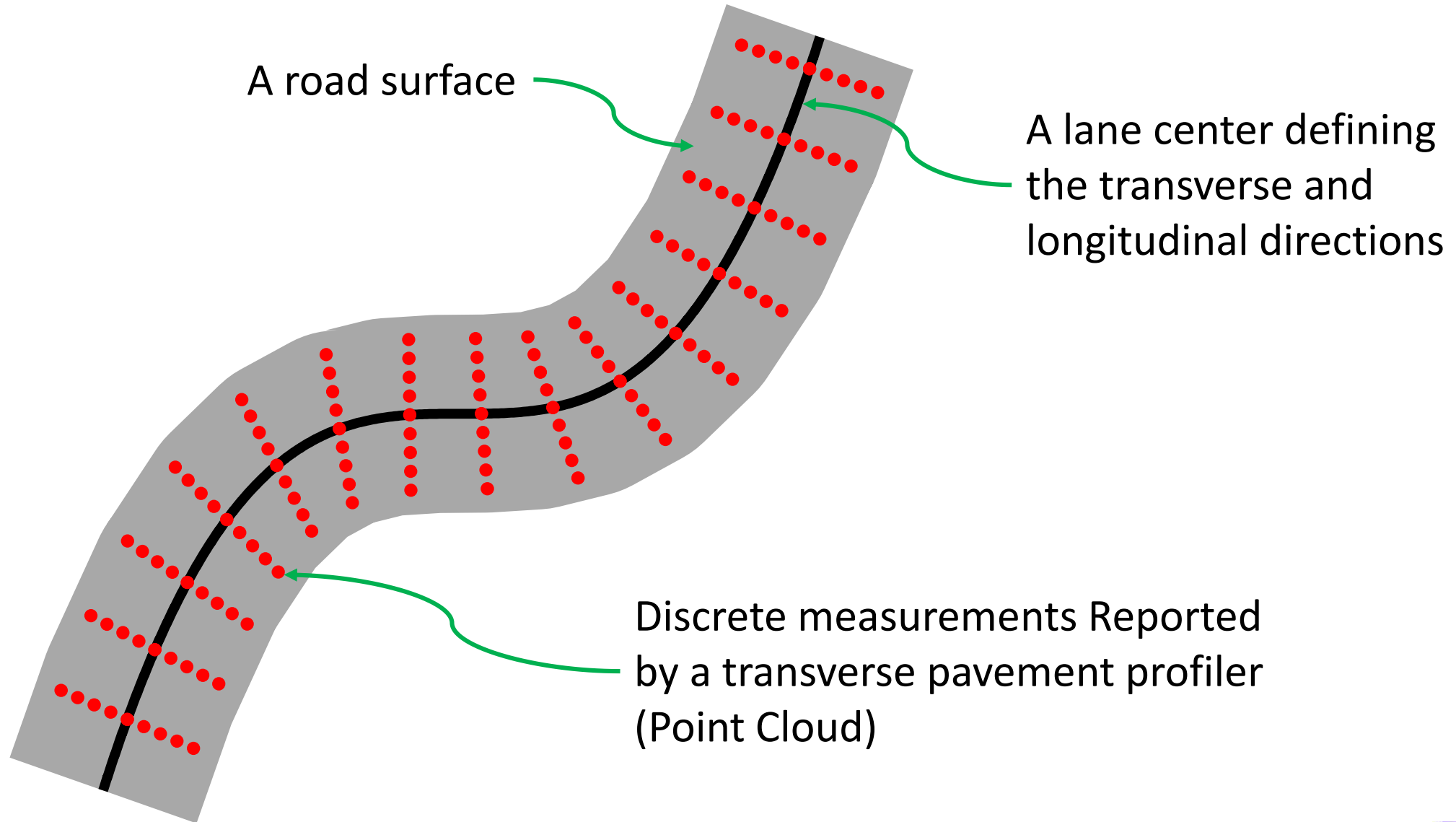
Vehicle Terrain Performance Laboratory  
Virginia Tech

# Objective

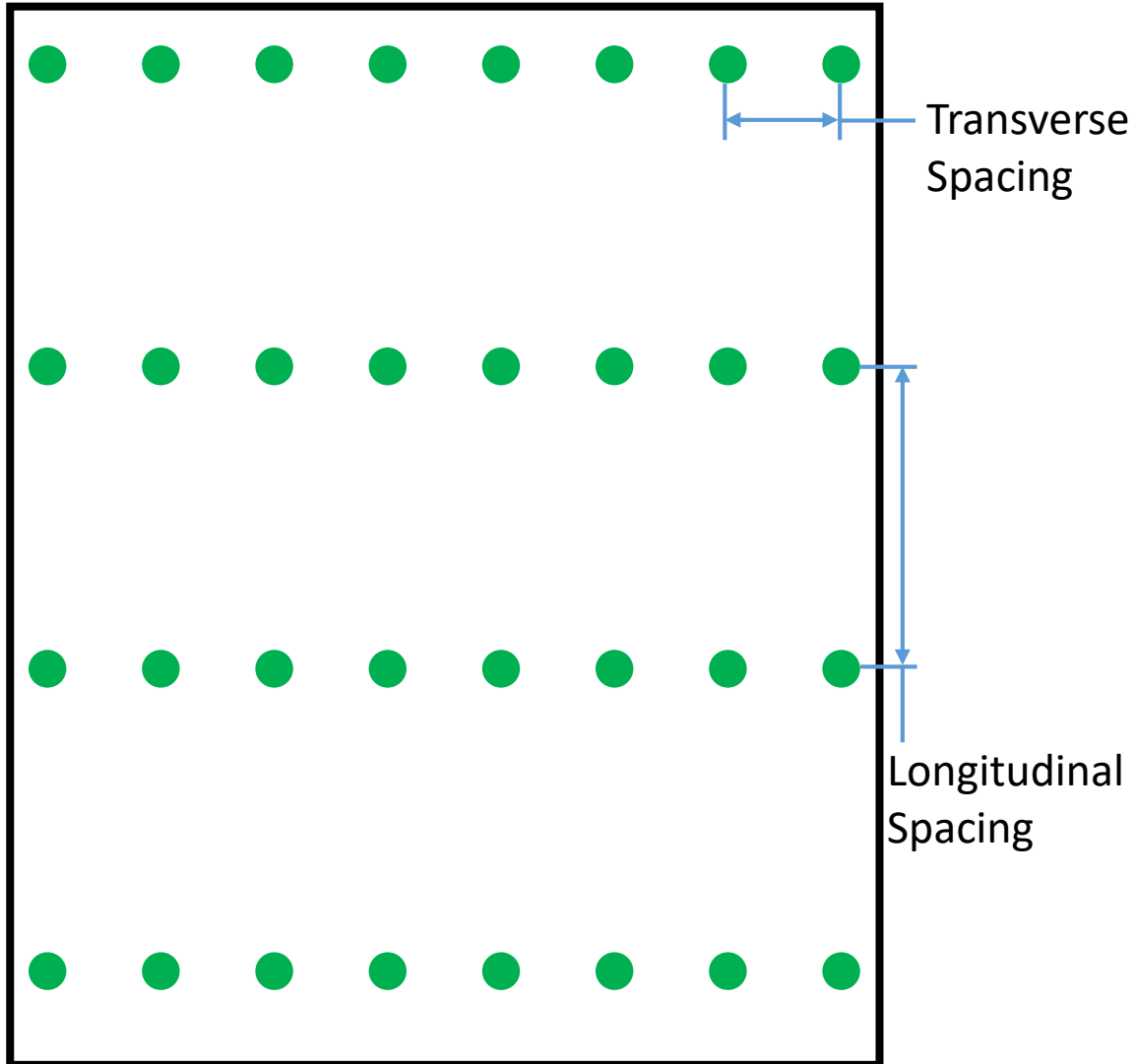
*Identify the **transverse** and **longitudinal** measurement spacing for a transverse pavement profiler*

- Need steamed from a FHWA Pooled Fund project
- Desired requirements:
  - Automated
  - Robust

# What information do we know?

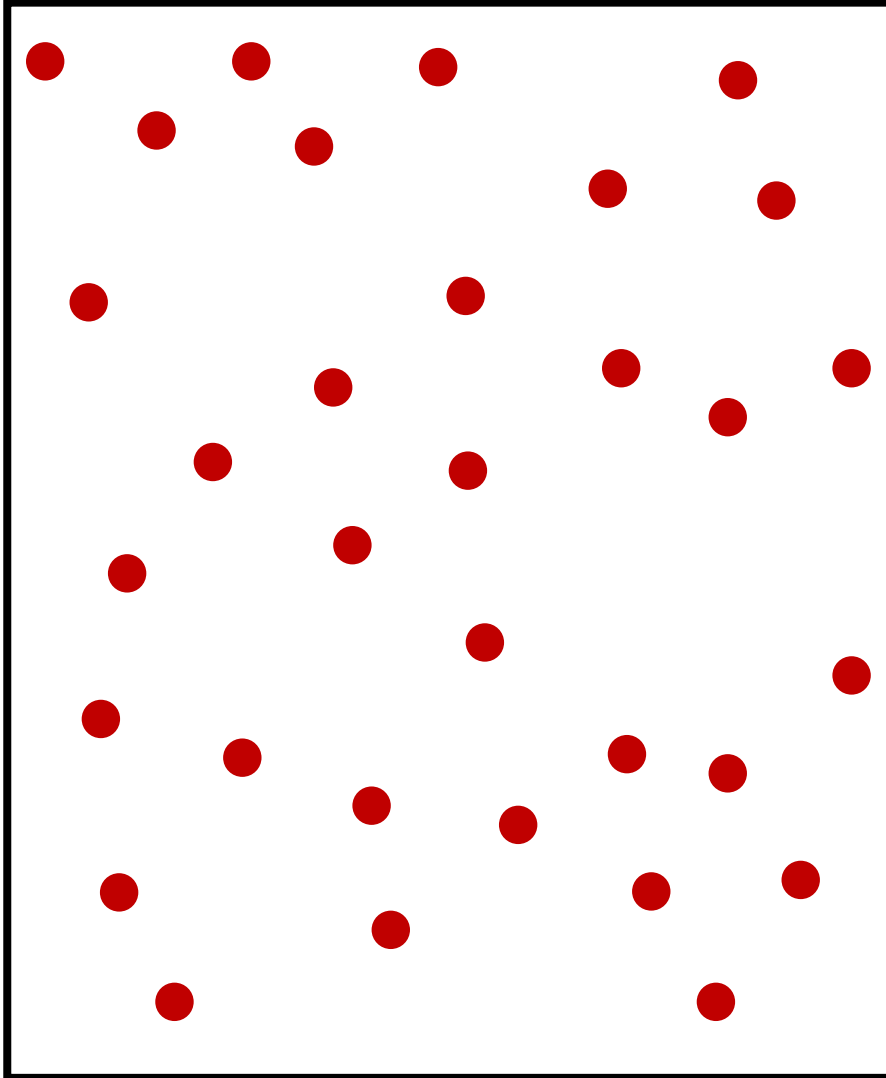


# Motivation: Road Scan 1



- Regularly Gridded Data
  - Uniform spacing
  - Easy to visually see the transverse and longitudinal spacing
  - Difference between neighboring data points

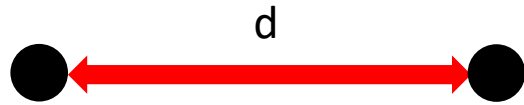
# Motivation: Road Scan 2



- Irregularly Spaced Data
  - What's the transverse spacing?
  - What's the longitudinal spacing?
  - No visual way of telling what the spacing is

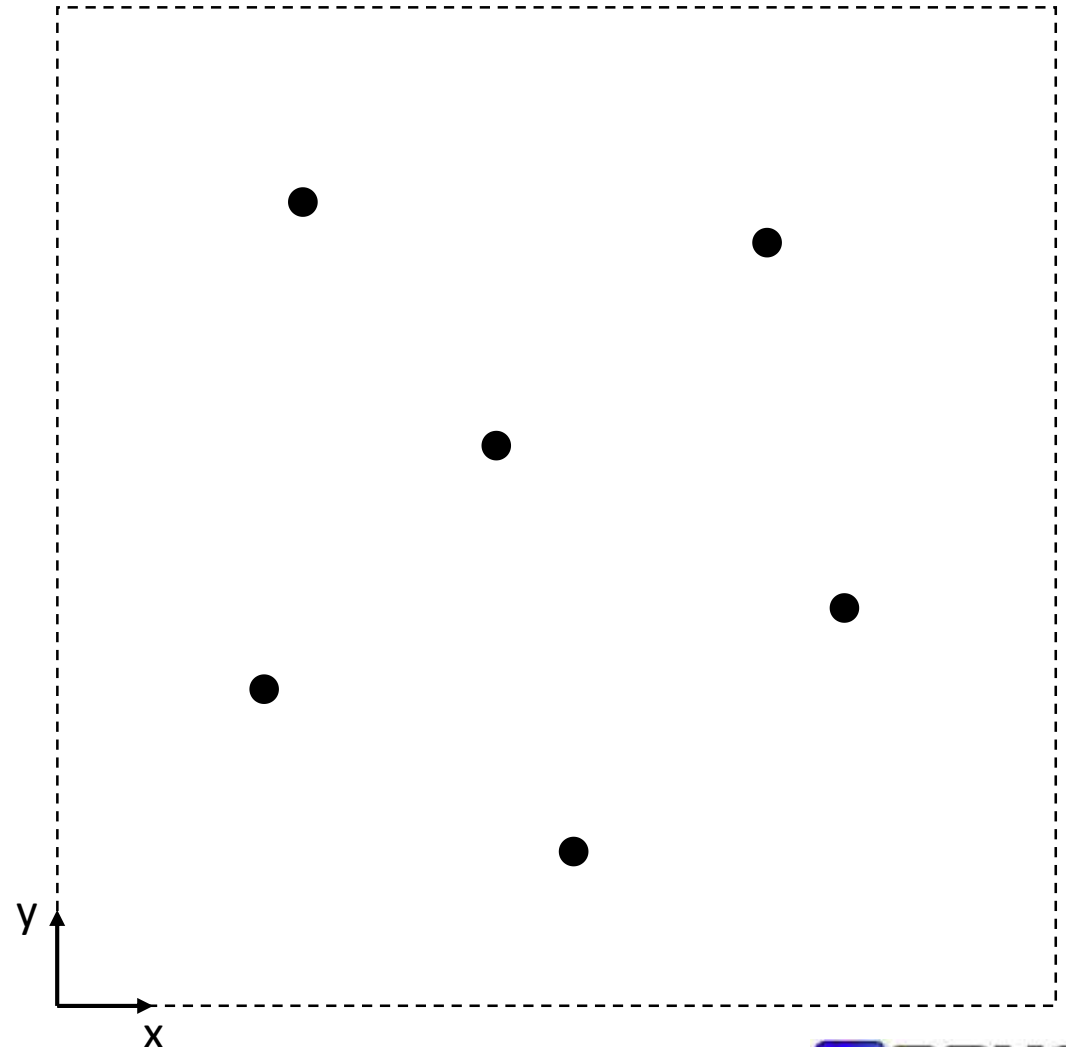
# Background: Nominal Point Spacing (NPS)

- A single representative distance between measurements in a point cloud



- Bounds on the smallest spatial feature which can be extracted.
- There are several methods for calculating the NPS

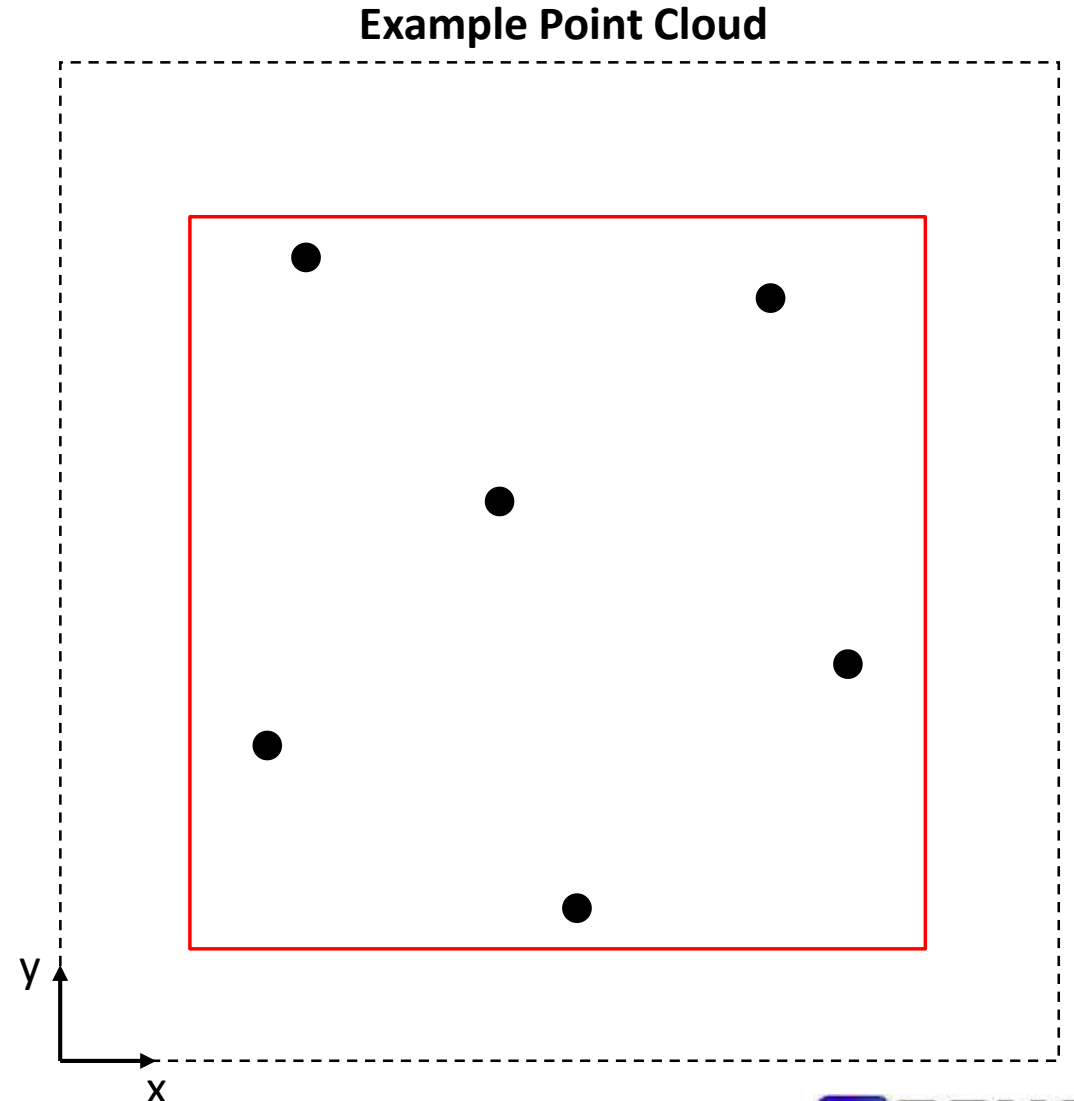
Example Point Cloud



# Background: Calculating NPS

## Averaging Method

- Define a local area of a point cloud using a polygon
- Identify the point density
  - $$\text{Density} = \frac{\text{Number of Measurement Points}}{\text{Area of a Prescribed Polygon}}$$
- Average NPS
  - $$\text{NPS} = \frac{1}{\sqrt{\text{Density}}}$$



# Background: Calculating NPS

## Voronoi Diagram

- Create a Voronoi diagram for a given point cloud
  - Unique polygon around each point

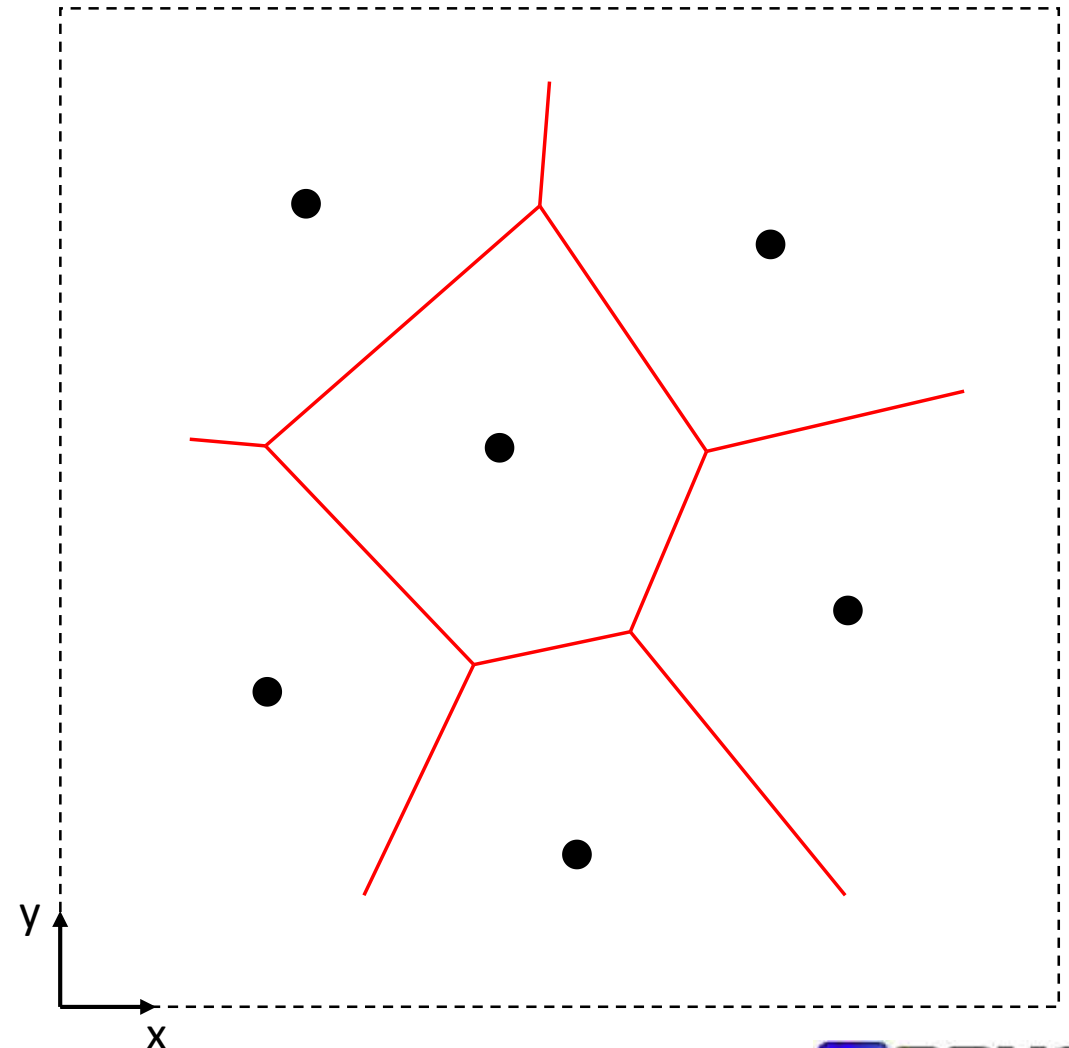
- Identify the point density

- Density =  $\frac{1}{\text{Voronoi Polygon Area}}$

- Average NPS

- NPS =  $\frac{1}{\sqrt{\text{Density}}}$

Example Point Cloud





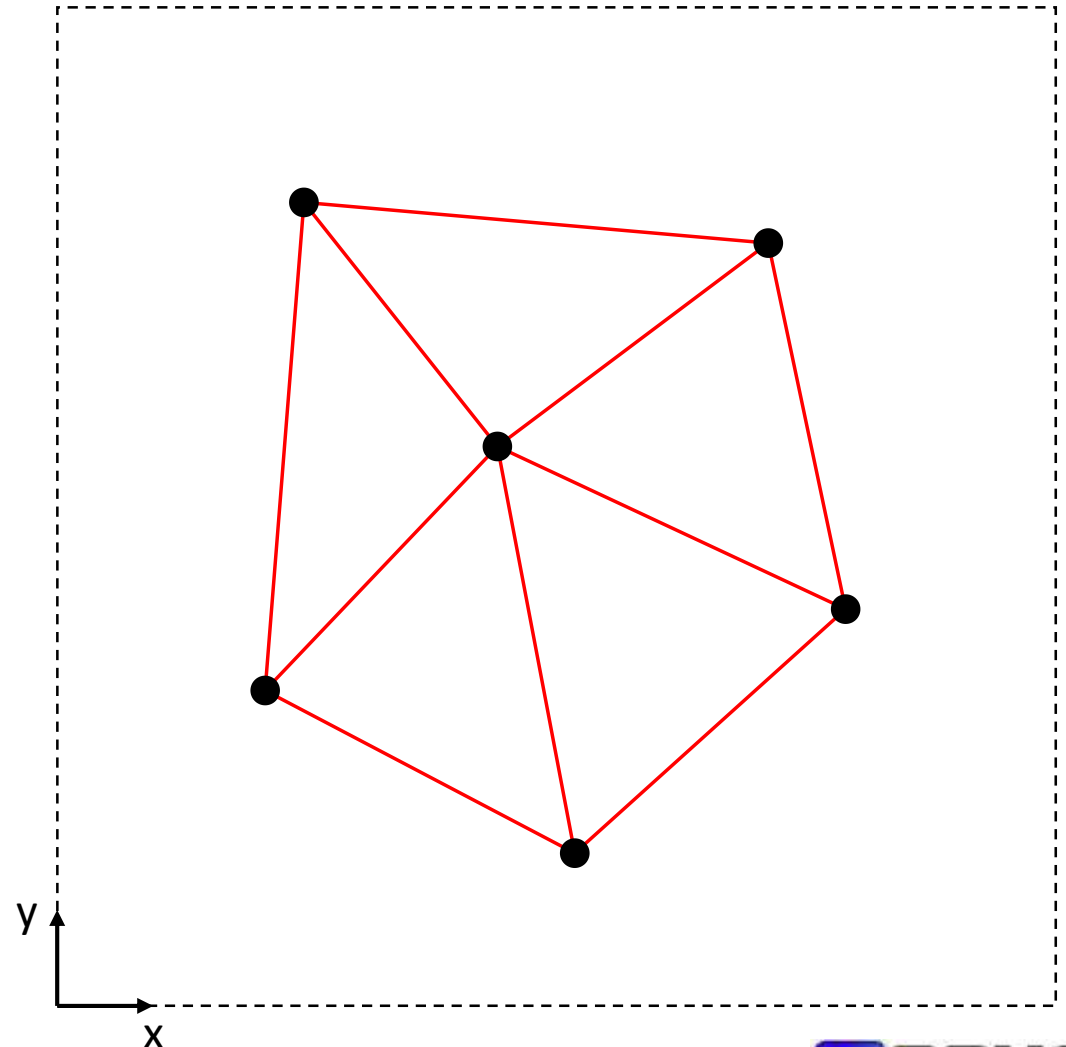
# Background: Calculating NPS

## Delaunay Triangulation

- Create a Delaunay Triangulation between all point cloud points
  - Triangles between points
  - No lines of the triangles cross
- Per measurement point calculate the average edge length to all nearby points

- $$\text{NPS} = \frac{[d_1 \ d_2 \ d_3 \ \dots d_N]}{N}$$

Example Point Cloud

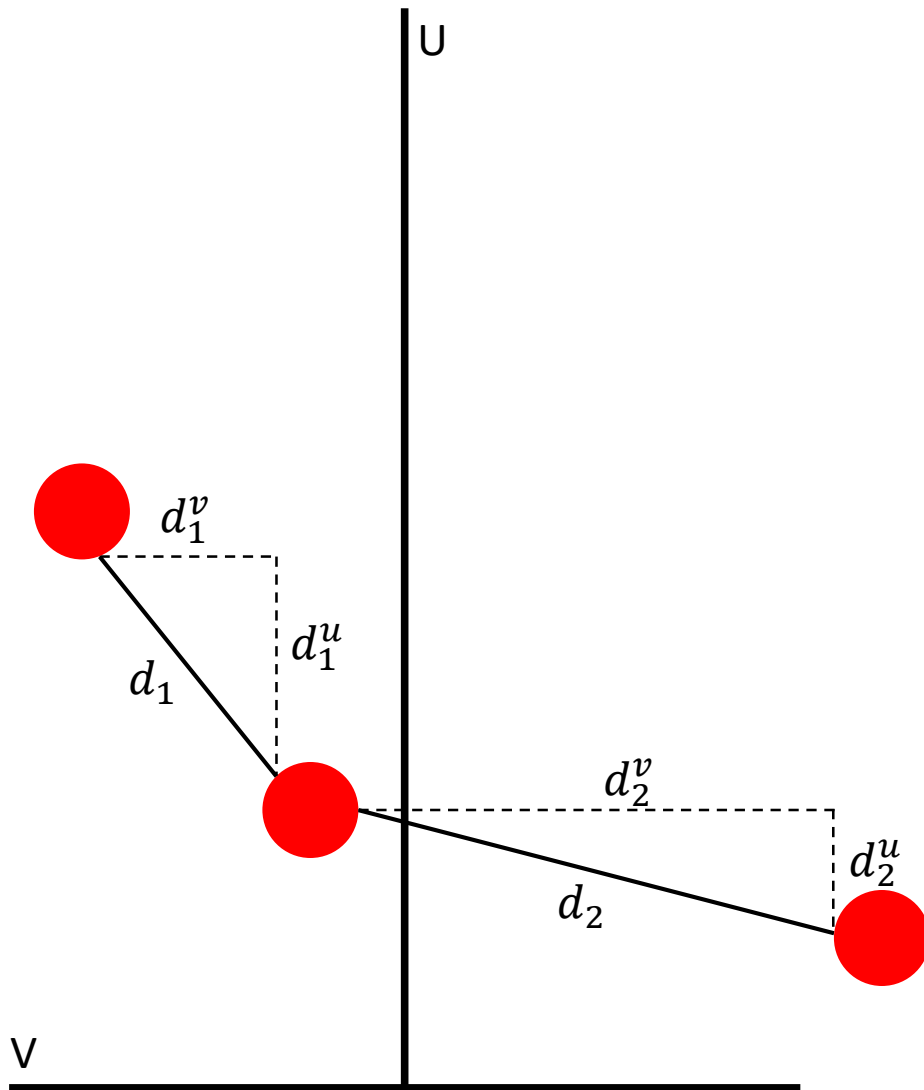


# Background: Calculating NPS

## Summarizing Comments

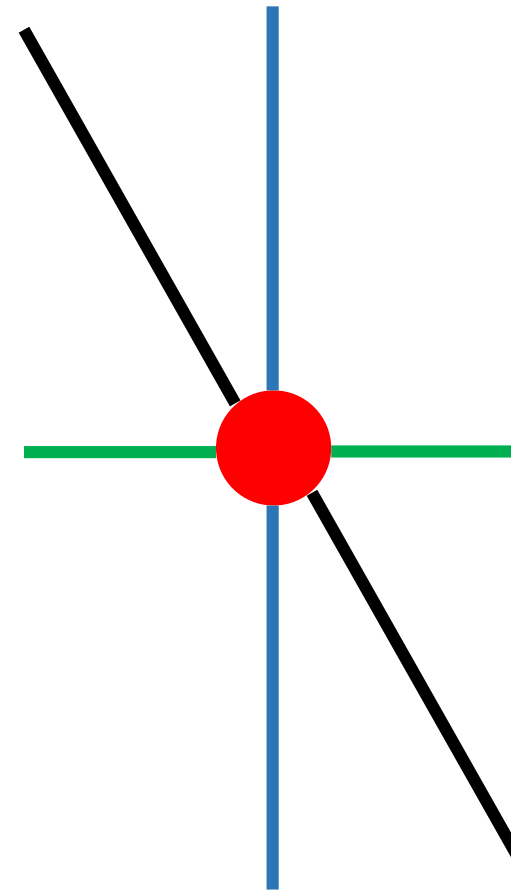
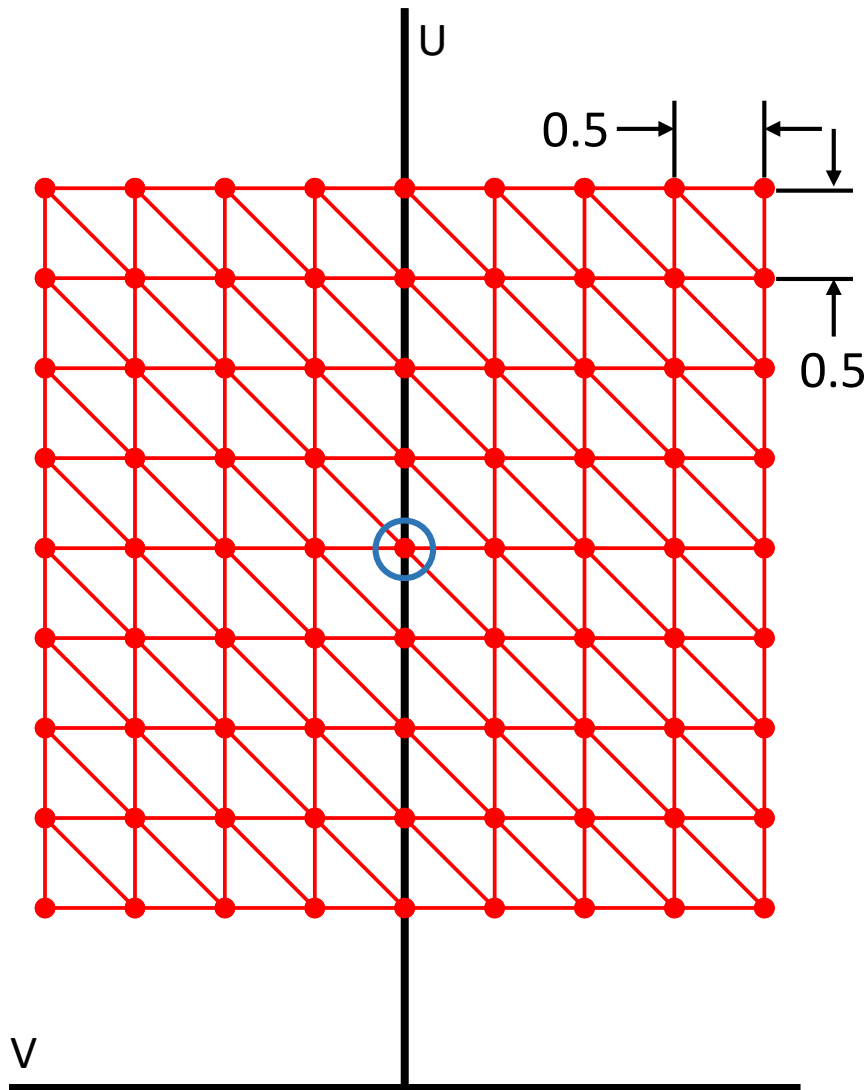
- Draw back of NPS in general
  - Only a single measure is established (no direction is considered)
- Averaging Method and Voronoi Diagrams calculate an average density
- Delaunay triangulation provides a means of identifying a distance between measurements

# Altering for our Application



- All measures can be considered in a path coordinate system
  - V – Transverse Direction
  - U – Longitudinal Direction
- Each Delaunay edge can be projected onto the (U, V) coordinate system

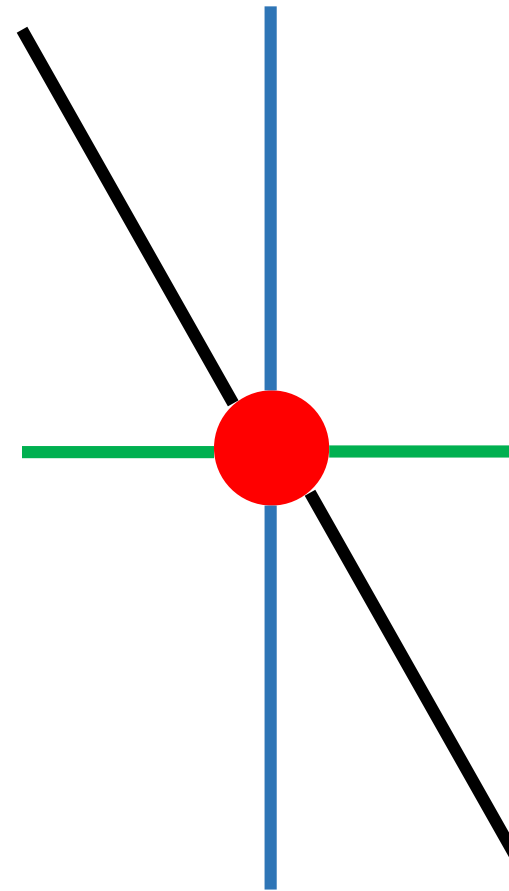
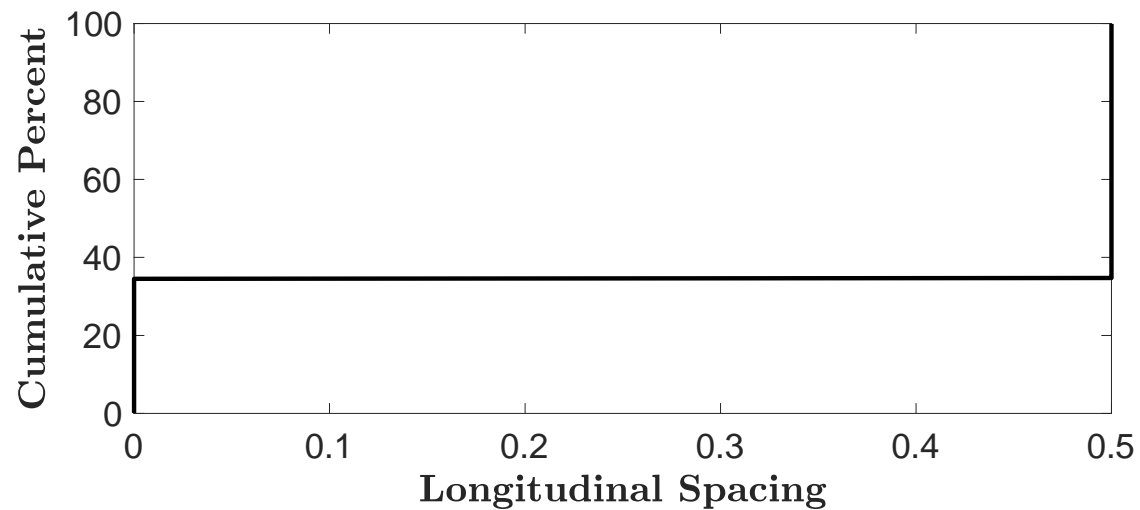
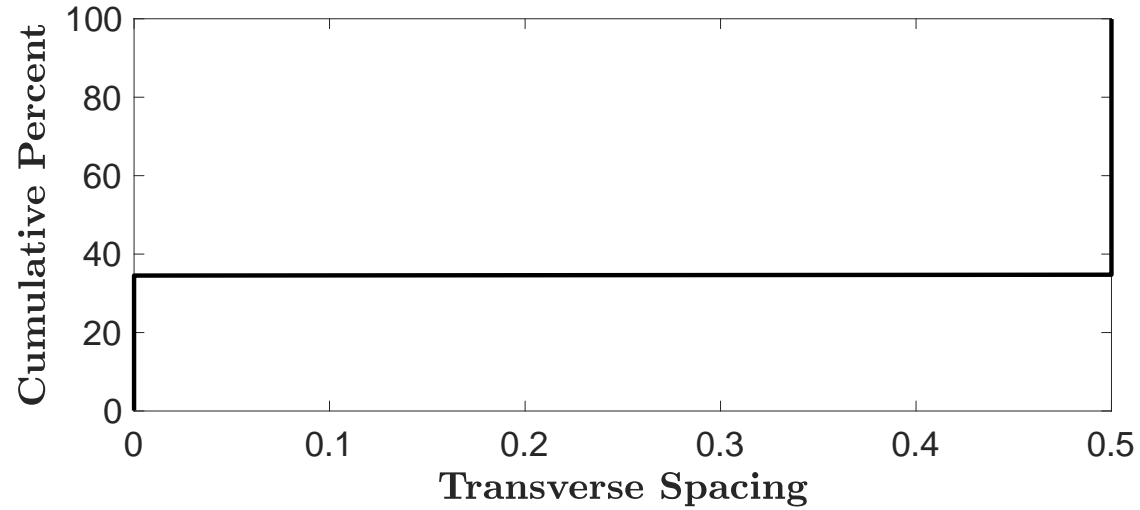
# Regularly Spaced Data



## Node Properties:

- 6 Delaunay edges
- 2 Transverse edges
- 2 Longitudinal edges
- 2 Angled edges

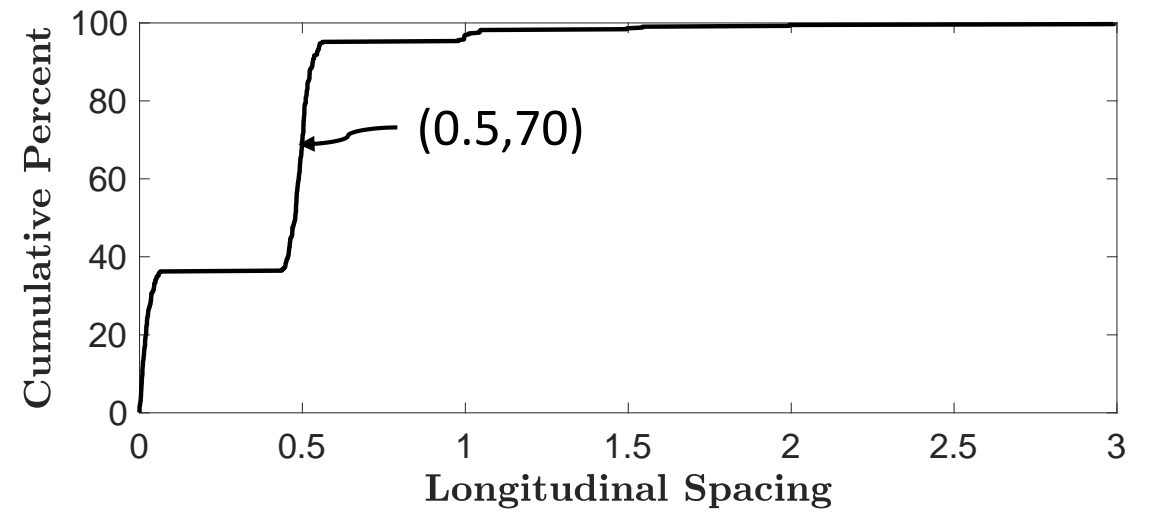
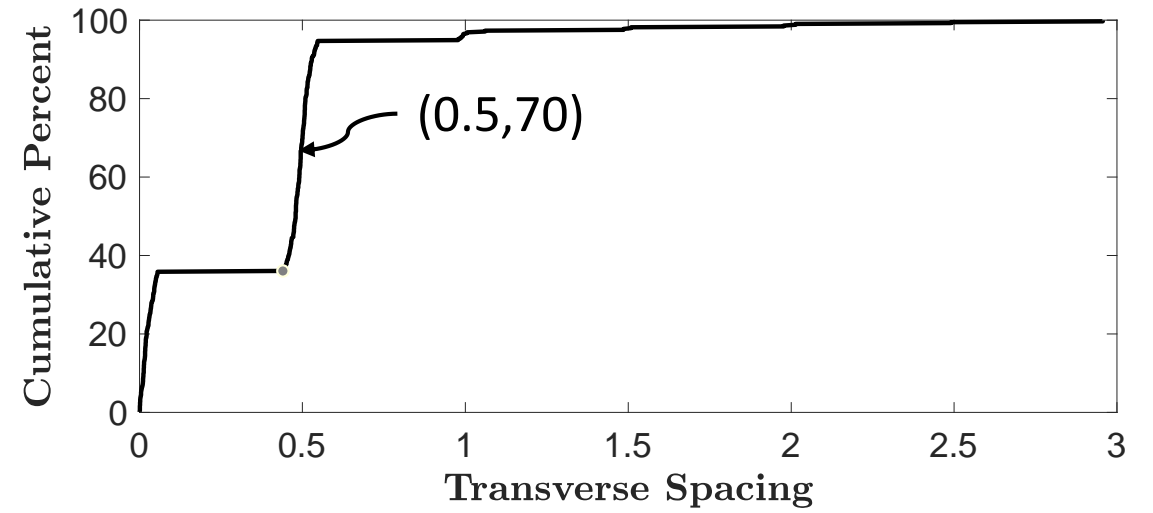
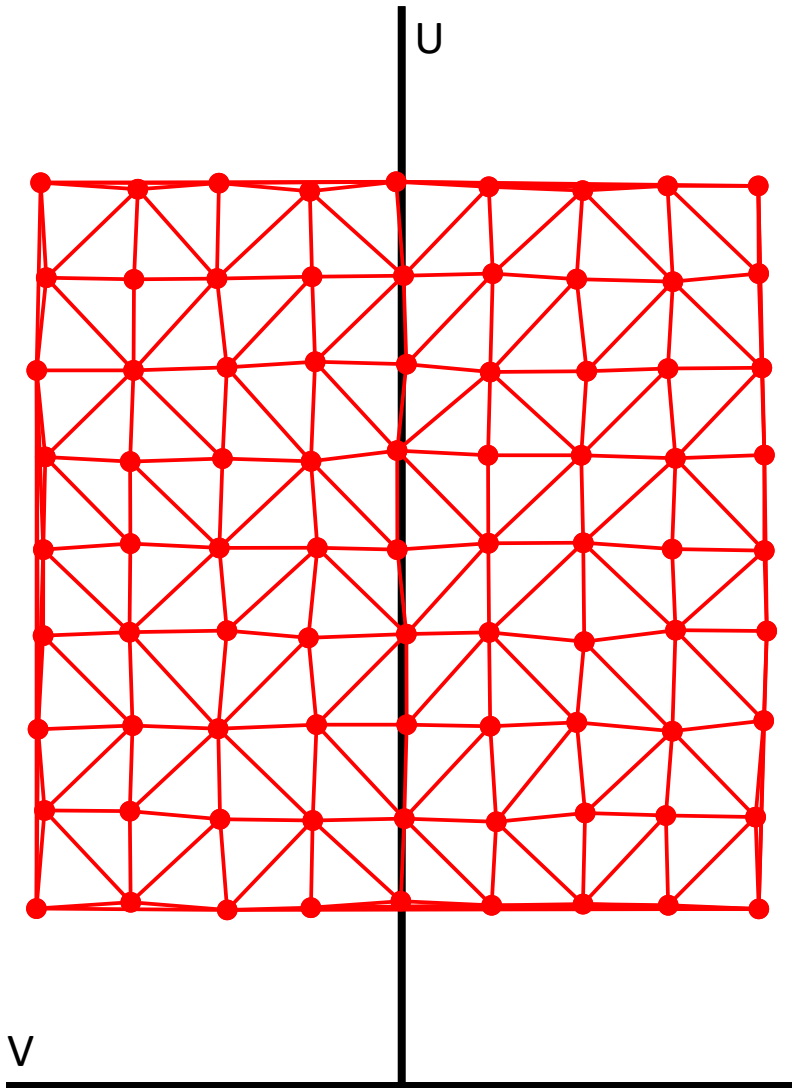
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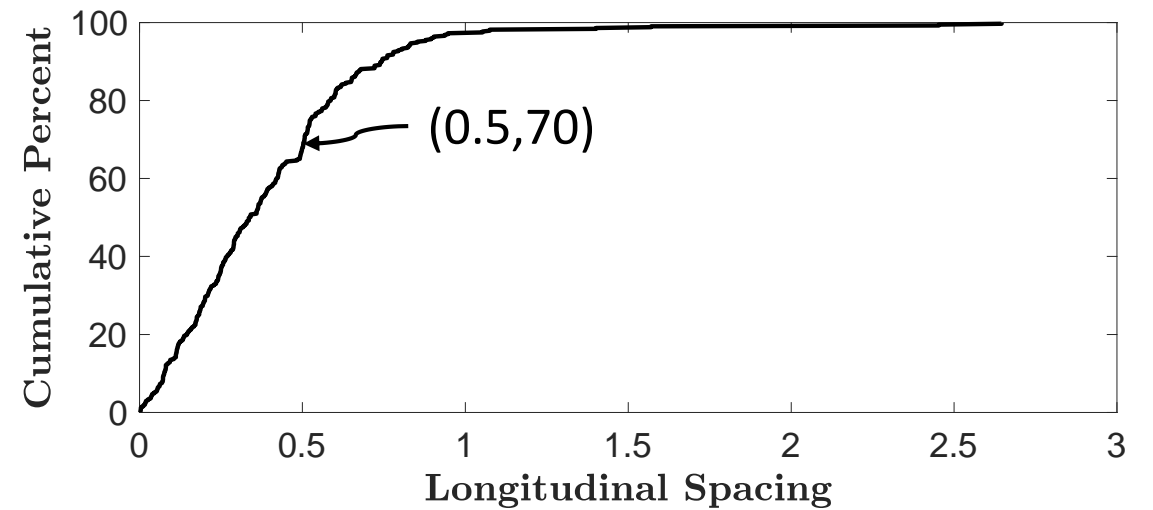
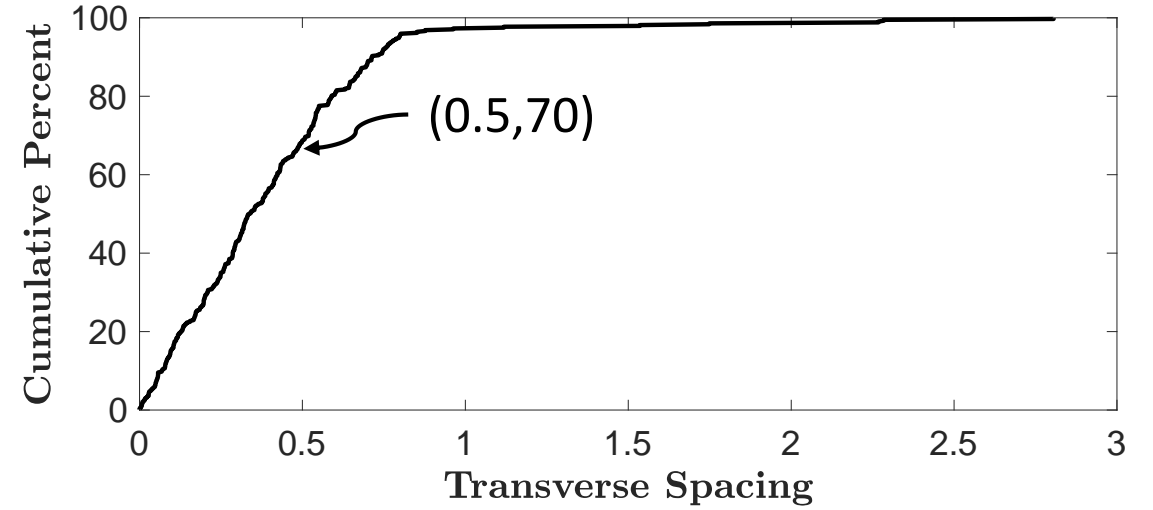
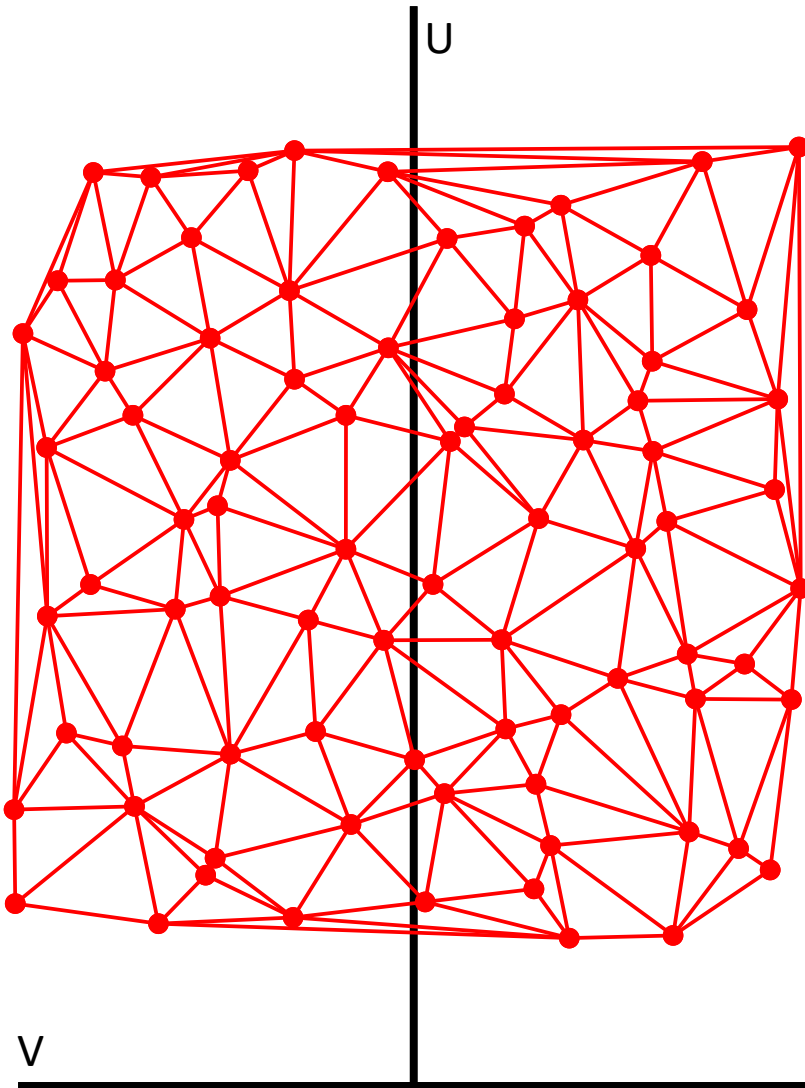
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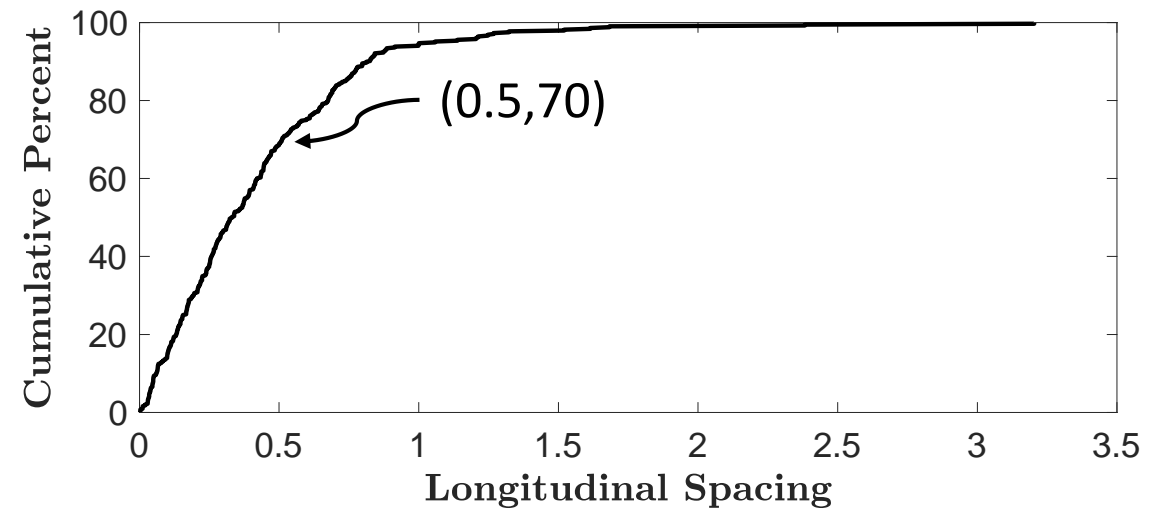
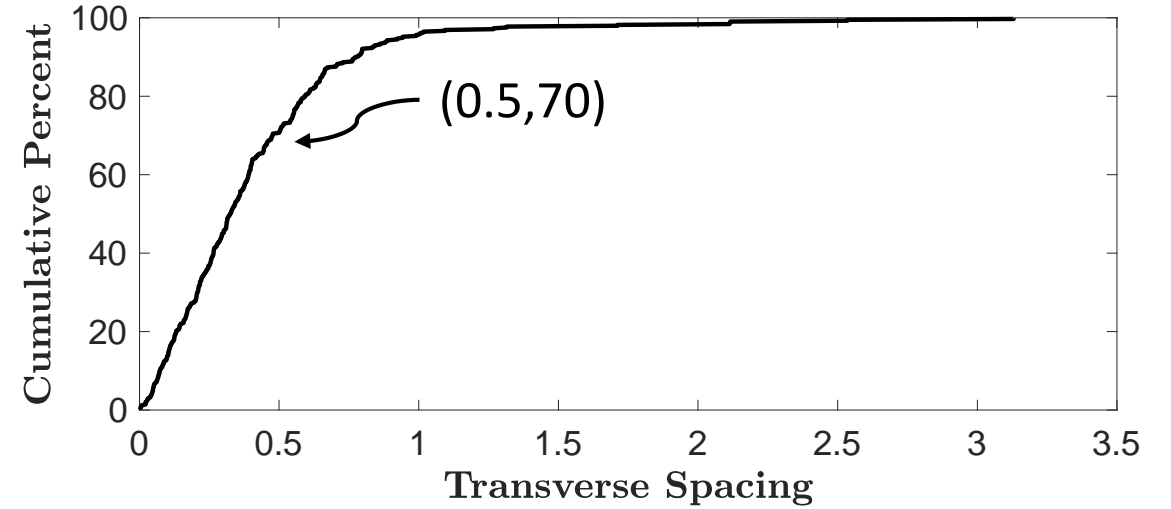
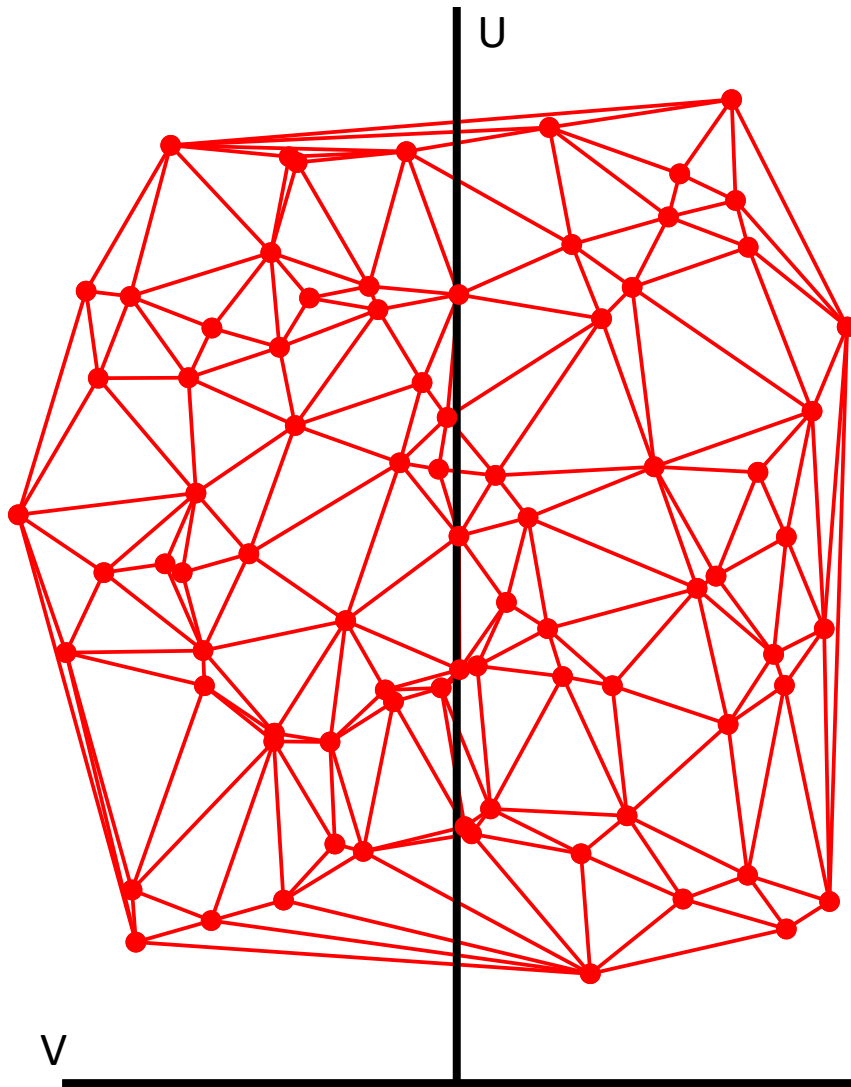
# Add a Little Noise



# Add More Noise



# Completely Random Data





# Concluding Statements

- Delaunay triangulation allows for connections to be made between measurements regardless of the spacing
- Each Delaunay edge can be projected onto the transverse and longitudinal axes
- There is still work to be performed before this analysis method can be implemented